

This is with mkii:

$$\left\| \int_0^1 G(\cdot, s) ds \right\|_{L^q} \lesssim \|G\|_{L^p}.$$